COSC581 - Algorithms Spring 2023 Homework #7

Due: Tuesday, 03/28/2023, before class.

- 1. Give an example of a linear program for which the feasible region is not bounded, but the optimal objective value is finite.
- 2. Write a linear program formulation corresponding to finding the maximum flow in the figure below. You do not need to solve the linear programming formulation.



- 3. Use the simplex method to solve the following linear programming formulations:
 - a. Minimize $-5x_1 + 3x_2$, subject to:

$$x_1 - x_2 \le 1$$

 $2x_1 - x_2 \le 2$
 $x_1, x_2 \ge 0$

b. Maximize $5x_1 + 4x_2 + 3x_3$, subject to: $2x_1 + 3x_2 + x_3 \le 5$ $4x_1 + x_2 + 2x_3 \le 11$

$$3x_1 + 4x_2 + 2x_3 \le 8$$
$$x_1, x_2, x_3 \ge 0$$